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**Article** 

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# Noise-immune quantum correlations of intense light

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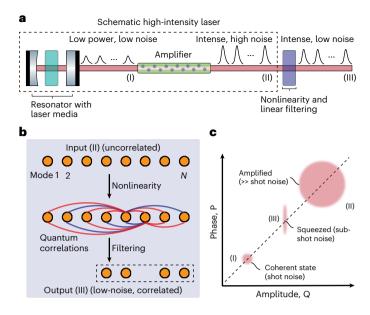
Lasers with high intensity generally exhibit strong intensity fluctuations far above the shot-noise level. Taming this noise is pivotal to a wide range of applications, both classical and quantum. Here we demonstrate the creation of intense light with quantum levels of noise even when starting from inputs with large amounts of excess noise. In particular, we demonstrate how intense squeezed light with intensities approaching 0.1 TW cm<sup>-2</sup>, but noise at or below the shot-noise level, can be produced from noisy inputs associated with high-power amplified laser sources (an overall noise reduction of 30-fold). On the basis of a new theory of quantum noise in multimode systems, we show that the ability to generate quantum light from noisy inputs results from multimode quantum correlations, which maximally decouple the output light from the dominant noise channels in the input light. As an example, we demonstrate this effect for femtosecond pulses in nonlinear fibres, but the noise-immune correlations that enable our results are generic to many other nonlinear systems in optics and beyond.

Lasers are among the most important inventions of the twentieth century, with innovations continuing more than 60 years after the demonstration of the first laser. While lasers are much more stable than the thermal light sources preceding them, their intensity and phase still fluctuate, owing to both external sources and intrinsic quantum-mechanical effects. In many settings, including metrology<sup>1-3</sup>, quantum state preparation<sup>4</sup> and biomedical imaging<sup>2,3,5</sup>, it is important to have both high intensity and low intensity fluctuations, for example, at, or even below, the shot-noise level associated with the quantum-mechanical coherent states of Glauber. For shot noise (equivalently, Poissonian statistics), the variance  $(\Delta n)^2$  in the detected photon number n is given by  $(\Delta n)^2 = \langle n \rangle$ , with  $\langle n \rangle$  being the mean photon number.

For lower-intensity lasers, such as continuous-wave sources based on stable optical oscillators, the intensity noise often follows

the expectation from Poisson statistics. By contrast, higher-power laser systems—which are often based on amplification of a lower-intensity laser<sup>6</sup> as shown in Fig. 1a—tend to deviate from Poissonian statistics, frequently showing intensity fluctuations orders-of-magnitude in excess of the shot-noise limit. This excess noise often comes from the amplifier, where it is known that for a linear phase-insensitive amplifier, the intensity variance scales as the square of the power gain<sup>7,8</sup>. Various techniques exist to control noise, such as linear filtering<sup>9</sup>, active feedback<sup>10</sup> or passive techniques based on second- or third-order optical nonlinearities<sup>11–13</sup>. However, these techniques are often unable to achieve sufficient noise reduction, particularly when the initial noise level is high, without extreme attenuation. As a result, it is difficult to produce light with high intensity and quantum levels of noise. Addressing this roadblock could enable, beyond the applications described

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**Fig. 1**| **High-intensity sources of light with quantum levels of noise. a**, A typical high-intensity laser system is realized by amplifying the output of a lower-intensity laser, which can generate approximations of coherent states. After amplification, the intensity and noise are both strongly enhanced. By subjecting the output of a high-intensity source to nonlinearity, such as third-order nonlinearity plus mode-selective filtering, one can lower the noise considerably with modest attenuation—in some cases producing quantum light, such as squeezed states, from noisy inputs. b, The principle for noise reduction is that nonlinearity creates quantum intensity correlations between different modes (yellow circles) in the laser field (red line, positive correlation; blue line, negative). Filtering through a subset of those modes can lead to an output whose correlations 'conspire' to make the remaining modes immune to noise at the input. c, The noise at various stages in a is shown in terms of phase space distributions. In this work, we demonstrate the step from (II) to (III).

above, a wide range of new techniques for generating quantum states of light<sup>14–16</sup>, as well as quantum states of excitations in materials such as electrons<sup>17,18</sup> and phonons<sup>19,20</sup>—based on strong-field driving, where the needed intensities are achievable, but the requisite noise levels are yet out of reach.

Our work is based on a surprising discovery that intense pulses propagating through a nonlinear medium can emerge with fluctuations at or below the shot-noise level (in a squeezed state), despite having initial fluctuations far above the shot-noise limit. This is realized with much lower attenuation than when using pure linear attenuation for noise reduction. We demonstrate this effect and uncover its origin, as a carefully tuned combination of nonlinear dynamics and linear attenuation. Understanding its origin enables us to maximize the squeezing and intensity simultaneously, reaching noise reduction conditions that exceed by nearly an order of magnitude the noise reduction expected from pure linear attenuation of the same magnitude. This approach let us create pulses with focusable intensities on the order of 0.1 TW cm $^{-2}$ , with measured noise 4 decibels (dB) below the shot-noise level.

To capture the entire picture, we build a new theory of quantum noise in multimode nonlinear systems, with which we show that the nonlinear dissipation process producing the squeezed light is essentially immune to the addition of noise in the pump. Consequently, the output noise is largely independent of the input level of noise. This noise-immune squeezing is a collective effect, arising from correlations between different modes created by nonlinearity: while any individual mode has strong noise, a group of modes, together, can almost completely decouple from noise, even in the noisiest channels of the input. We call these noise-immune quantum correlations. Our results—demonstrated for the example of femtosecond pulses propagating through

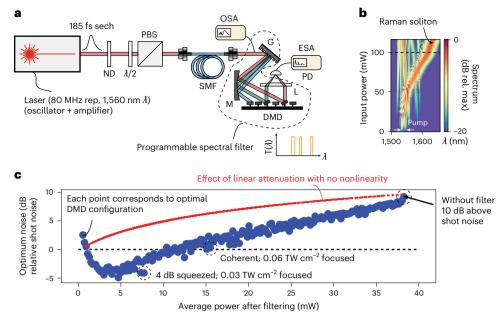
an optical fibre—are general, applying to a wide range of nonlinearities that create quantum correlations between different modes.

#### Results

We start by illustrating the core concept of this work: that although high-intensity lasers generally have noise exceeding the shot-noise limit of coherent states, nonlinear effects can lead to noise reduction below the shot-noise limit while retaining substantial intensity. High-intensity laser systems are typically realized by amplifying the output of a lower-intensity laser. While the output is also intense, the intensity fluctuations are much larger than the shot-noise level (Fig. 1a,c). In this work, we will consider what happens when the output of an amplified high-intensity laser goes through a nonlinear filtering or nonlinear dissipation process, which we define as any process that is both nonlinear in the complex amplitudes of the input, and changes (reduces) the intensity of the output relative to the input. The intensity must change: otherwise, the intensity fluctuations cannot change. The effect of the nonlinearity will be to induce quantum correlations between different degrees of freedom (modes) in the pulse (Fig. 1b). Here we show data for the example where the modes are frequency components of a propagating pulse confined to a single transverse mode. However, the concept also holds when the different degrees of freedom involve spatial modes, polarization and so on. The filter after the nonlinearity down-selects a subset of correlated modes, which, as we will explain later in the text, are maximally insensitive to noise in the initial pulse. When the insensitivity is sufficiently strong, the noise at the output becomes independent of the noise at the input, permitting the conversion of light far above the shot-noise level into light far below it (corresponding to intensity squeezing). In contrast to previous work exploring squeezing by spectral filtering<sup>21,22</sup> of fundamental N = 1 solitons <sup>9,23–25</sup>, we operate in a regime of much higher power (beyond the regime of fundamental solitons; Fig. 2b) and much higher initial noise levels, allowing us to demonstrate and elucidate the general concept of noise-immune squeezing of intense light, which is the crucial step to high-intensity lasers with quantum levels of noise.

We show this effect experimentally. For the amplified laser system, we use a commercial femtosecond pulsed laser system, which comprises a low-noise oscillator and an erbium-doped fibre amplifier. The resulting pulses are sent through a single-mode fibre (with anomalous dispersion at the centre wavelength of the pulses, 1,560 nm), which provides nonlinearity. The pulses are then sent into an arbitrarily programmable spectral filter shown in Fig. 2a: the fibre and filter realize the nonlinear dissipation process. In particular, the filter selects a subset of wavelengths, which are correlated owing to the nonlinearity, acting as a realization of Fig. 1b. Four-wave mixing and dispersion in the fibre, at high peak pulse intensities, lead to a splitting of the spectrum into a red-shifted soliton (called the Raman soliton), and a highly modulated, chaotic part near the wavelengths of the initial pulse, which we refer to as the pump wavelength (Fig. 2b).

Now, we show the effect of filtering after the nonlinearity. Let us consider the space of spectral filters that have the same output power after the filter. For a given output power, there will be an optimal filter that realizes the lowest intensity fluctuations. In general, the noise of the nonlinearly filtered output is much lower than can be realized by simple broadband linear attenuation alone: at some powers, the difference is approximately an order of magnitude. Moreover, after attenuation, the outputs can be at or below the shotnoise level, nearly 5 dB below the standard quantum limit, despite the input to the nonlinear filtering process having intensity noise that is 10 times the shot-noise limit (Fig. 2c). The shot-noise level is determined based on the known scaling of noise with linear attenuation for shot-noise limited light. Despite attenuation, the peak powers and focusable intensities are high, on the order of 1 kW and 0.1 TW cm<sup>-2</sup>, respectively.



**Fig. 2**| **Generating intense squeezed light from noisy amplified sources. a**, Light passes through a single-mode fibre (SMF) and then the output pulse is passed through a programmable spectral filter (of resolution 1.33 nm) realized by a grating (G)—mirror (M) pair and a digital micromirror device (DMD). The filtered pulse is sent to a photodiode (PD) and its noise is measured with an electronic spectrum analyser (ESA). The attenuation in the free-space region between the exit of the fibre and the photodetector is 34%. **b**, Spectrum of light passing through the fibre as a function of average power. The dashed line represents the input power that we work at for the remainder of the text. rel., relative to. **c**,

Minimum noise of the light after filtering (blue points), relative to shot noise, as a function of average power transmitted by the filter. The red curve represents the result of frequency-independent linear loss on the output, showing that spectral filtering after nonlinearity leads to much stronger noise reduction and even squeezing, starting from a pulse with noise 10 dB above the shot-noise level. The focused intensity is defined as the peak intensity divided by  $\pi\lambda^2/4$ . Legend for additional elements in **a**: filter (ND), half-wave plate ( $\lambda/2$ ), polarizing beam splitter (PBS), lens (L) and optical spectrum analyser (OSA).

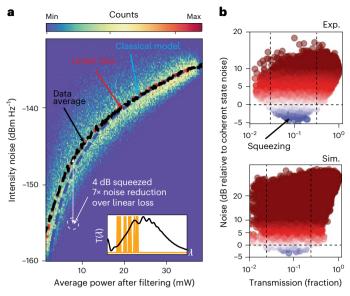
Not all filters lead to noise reduction, despite reducing the overall intensity (reducing the intensity by two reduces the intensity noise by two for shot-noise limited light, and four for light with noise far above shot noise). A randomly chosen filter is about as likely to increase the noise as it is to decrease it: see Fig. 3a, where we plot the output power and intensity noise after a large number of randomly chosen spectral filters (Fig. 3b (top) shows the same result normalized to shot noise). The minimum noise for each output power corresponds to Fig. 2c. Even for very low attenuation, the noise can decrease or increase by about 3 dB. For larger degrees of attenuation, the noise after nonlinear filtering can even increase by an order of magnitude relative to the expectation from linear loss. An example of a filter that leads to strong noise reduction is shown in the inset of Fig. 3a, overlaid on the red-shifted solitonic part of the spectrum in Fig. 2b. The filters that lead to noise reduction overwhelmingly concentrate transmission on the red-side of the solitonic peak. They also tend to feature spectral gaps: without this, noise reduction is not realized.

We now describe the physical mechanism underlying the 'noise-immune squeezing' behaviour that we have observed. We start by presenting a general framework that we have developed to predict noise in multimode nonlinear systems (even applying to nonlinear systems beyond optics). The theory lets us predict quantum noise purely from classical modelling of the nonlinear dynamics, bypassing second quantization altogether, while nevertheless accurately predicting quantum effects such as squeezing, entanglement and so on. It is important to emphasize that while our framework appears semi-classical, our general result is equivalent to the rigorous quantum-mechanical results, in the regime where intensity fluctuations are small compared with the mean intensity. To make this point more clear, in Supplementary Information (Supplementary Section 2), we also explicitly show a few cases where we compare the predictions of our framework against

the standard quantum-mechanical approach with operators: in all cases, they exactly agree.

Applied to our experimental results: by calculating the classical dynamics of femtosecond pulses in a fibre, according to the generalized nonlinear Schrodinger equation (GNLSE; Supplementary Section 3)—as is done in all classical work on pulse propagation in fibres—and calculating the derivative of the filtered output intensity with respect to all possible changes in the initial conditions, one can predict quantum noise, bypassing standard approaches such as linearized Heisenberg equations, or stochastic equations. Among the major advantages of our framework, which we call quantum sensitivity analysis, are as follows: (1) the resulting noise expressions are directly understood in terms of the classical dynamics, leading directly to new insights, and (2) the framework efficiently and analytically predicts output noise for arbitrary input noise profiles, which is challenging for the other methods but necessary for developing intense quantum light.

While a detailed derivation of the most general form of the theory is provided in Supplementary Information (Supplementary equations (S5) and (S9)), we present a key special case here, connecting the variance of any property of the output to derivatives of the classically predicted output with respect to the initial conditions. A wide variety of classical nonlinear dynamical systems can be mathematically specified as an initial-value problem, transforming a set of inputs to a set of outputs. Denote the inputs  $\alpha_{\text{IN},i}$  and the outputs  $\alpha_{\text{OUT},i}$ , where i labels a degree of freedom (or mode) and  $\alpha$  denotes the value of that degree of freedom. For the system described in Figs. 2 and 3, where the classical dynamics are governed by the GNLSE, the modes i correspond to frequency components of the initial pulse, while the  $\alpha$  are the corresponding complex Fourier coefficients. In a general multimode system, the ican also include spatial modes, polarization and even material degrees of freedom. Any property of the output that we measure, denoted  $X_{\text{OUT}}$ 



**Fig. 3** | **Noise statistics of nonlinear filtering. a**, Filtered intensity (x-axis) and intensity noise (y-axis) for different randomly chosen filters. Inset: a type of filter (orange) overlaid on the output spectrum (black; the peak corresponds to the red-shifted peak in Fig. 2b), which leads to squeezing. **b**, Same as in **a** but with the intensity noise normalized to the shot-noise level associated with coherent states (top), compared with theory (bottom). The colour scale reflects the noise normalized to shot noise. The dashed lines mark the region of transmission that leads to observed squeezing. Exp., experimental; Sim., simulated.

(for example, total intensity of a filtered output pulse), is a function of the inputs:  $X_{\rm OUT} = X_{\rm OUT} [\{\alpha_{\rm IN}, \alpha_{\rm IN}^*\}]$ . Here we include the dependence on the complex conjugate fields, as they are in principle independent variables, being coupled by nonlinearity.

Assume that the input has noise in the different input modes, denoted  $\delta\alpha_{\text{IN},i}$ . In the absence of external noise sources, this noise comes only from vacuum fluctuations, described by noise correlations  $\langle \delta\alpha_{\text{IN},i}\delta\alpha_{\text{IN},j}^* \rangle = \delta_{ij}, \langle \delta\alpha_{\text{IN},i}^*\delta\alpha_{\text{IN},j}^* \rangle = \langle \delta\alpha_{\text{IN},i}\delta\alpha_{\text{IN},j} \rangle = \langle \delta\alpha_{\text{IN},i}^*\delta\alpha_{\text{IN},j}^* \rangle = 0$ . In the presence of additional noise, from amplifiers or external sources, the noise changes. Assuming that this noise is uncorrelated and phase insensitive, as is common in linear amplifiers, the variance in  $X_{\text{OUT}}$ , denoted  $(\Delta X_{\text{OUT}})^2$ , is given as (Supplementary Section 2):

$$(\Delta X_{\text{OUT}})^2 = \sum_{i} F_i \left| \frac{\partial X_{\text{OUT}}}{\partial \alpha_{\text{IN},i}} \right|_{\alpha_{\text{IN}} = (\alpha_{\text{IN}}), \alpha_{\text{IN}}^* = (\alpha_{\text{IN}})^*}^2.$$
 (1)

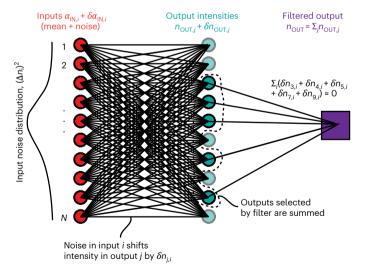
Here the derivative  $\partial X_{\text{OUT}}/\partial \alpha_{\text{IN},i}$  represents the sensitivity of the output quantity to changes in the initial conditions of the classical nonlinear dynamics (that is, it is a purely classical quantity). In addition, the quantity  $F_i$  is the Fano factor, which measures the deviation of input mode i from coherent-state statistics. Specifically, it is given by  $F_i = (\Delta n_i)^2/\langle n_i \rangle$ , where  $\langle n_i \rangle$  is the mean photon number of the ith mode and  $(\Delta n_i)^2$  is the variance. Importantly, even for vacuum states  $\langle n_i \rangle = 0$ ,  $F_i = 1$ , and there is a finite and non-negligible contribution to the noise, representing the transduction of quantum vacuum fluctuations of the input modes to the noise in the output quantity. We note that the sum over i is a generalized sum, which for systems with continuous degrees of freedom (such as pulses) is understood as an integral. Before moving on, we note that the expression above can be generalized to include correlated noise, but it is unnecessary to account for our findings.

The physics before filtering is best understood in the continuous basis of propagating modes of the fibre of different wavenumbers (and thus frequency, given the fibre dispersion relation). The key quantity of

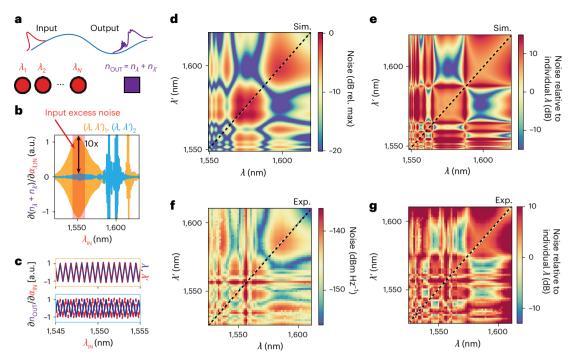
interest from the standpoint of filtering is the intensity–intensity correlation function. The correlation function should be understood as having a continuous wavelength domain. Because forward-propagating excitations of different wavenumbers are orthogonal linear modes, we can say that the continuous frequency basis is an orthonormal one. In other words, it is these individual propagating waves of different frequencies that are the 'modes' we refer to. However, once we start collecting light using optical systems with finite spectral resolution and analysis bandwidth, these well-defined degrees of freedom get mixed together via a linear transformation, and so the grating and digital micromirror device pick out linear superpositions of these frequencies. However, because the correlation function that we calculate is relatively smooth over one wavelength bin of our system, we approximate the continuous integral (which represents the truth) by a discrete sum.

In Fig. 3b (bottom), we used this framework to predict the random filtering experiment of Fig. 3a,b (top). The prediction is based on the framework described above. The overall trends, maximum squeezing and noise robustness are in excellent agreement. Importantly, the added noise cannot be removed trivially from the pump (for example, by filtering, as is often done in the presence of amplified spontaneous emission), since the added noise is at the wavelengths responsible for the nonlinear dynamics (the pump wavelengths).

Using this theory, we can now elucidate the mechanism of noise immunity and squeezing. According to equation (1), the noise in general increases when the excess noise in some input increases. Moreover, if the excess noise exists in multiple modes, that tends to enhance the noise as well. The only exception is if  $|\partial X_{\text{OUT}}/\partial \alpha_{\text{IN},i}| = 0$  over the range of input modes i where  $F_i > 1$ . This unusual broadband noise immunity requires looking at a property, which is a combination of different modes (sum of intensities of different Fourier components with different wavelengths, for example,  $X_{\text{OUT}} = \sum_{\lambda} n_{\lambda}$ ). In this case, fluctuations in the inputs lead to opposite shifts in different output modes, which cancel upon summation, leading to noise immunity, as illustrated in Fig. 4. This allows one to generate squeezing even from highly noisy



**Fig. 4** | **Noise immunity owing to multimode quantum correlations.** The noise in any output quantity such as the number of photons of a filtered output  $n_{\text{OUT}}$ , of a nonlinear interaction depends on both the magnitude of the noise (black curve) of the different input modes (red circles) and the sensitivity of the output to changes in the inputs. For an output that depends on multiple output modes, such as the sum of intensities in several modes (opaque teal circles), it is possible for a fluctuation in a mode i to lead to nearly zero shift in the sum of intensities (purple square), even if the individual modes shift strongly. This effect is due to quantum correlations created by the nonlinearity. Further, because of this perfect cancellation, the output noise is independent of the input level of noise.



**Fig. 5** | **Noise immunity for pairs of colours induced by quantum correlations. a**, Input–output formulation of ultrafast nonlinear dynamics of a femtosecond pulse in a fibre. The input modes are frequency components of the initial pulse. The output that we measure is the sum of intensities in two wavelength channels of the output. **b**, Simulated sensitivity of the total intensity in a pair of wavelengths for an input peak power of 4.1 kW, owing to fluctuations of the input wavelength channels, as a function of the input wavelength  $\lambda_{\rm IN}$ . The intensity of a typical pair of wavelengths  $(\lambda, \lambda')_1 = (1590, 1615)\,{\rm nm}$  (orange curve) shows a strong sensitivity to fluctuations in the wavelengths of the input pulse, shaded in red. The intensity in some special pairs  $(\lambda, \lambda')_2 = (1580, 1590)\,{\rm nm}$  (blue curve) shows strongly reduced sensitivity to changes in the input. **c**, The reduced

sensitivity occurs because a fluctuation at a given wavelength shifts the intensity in wavelengths  $\lambda$  and  $\lambda'$  oppositely for most fluctuation channels. Enhanced sensitivity comes from the same fluctuation of the input shifting the intensity in wavelengths  $\lambda$  and  $\lambda'$  in the same direction.  ${\bf d}$ , Theoretically predicted variance in the sum of intensities as a function of wavelengths  $\lambda$ ,  $\lambda'$ .  ${\bf e}$ , Noise relative to the less noisy of the two individual wavelengths. The signature of the cancellation in  ${\bf b}$  is a much reduced noise (blue regions in  ${\bf d}$ ) and a much lower noise than the individual intensities (blue regions in  ${\bf e}$ ).  ${\bf f}$ , Experimentally measured noise in the sum of intensities of different intensities.  ${\bf g}$ , Noise compared with the less noisy of the noise of the individual measured wavelengths.

inputs. Physically, in the case of femtosecond pulses in fibres, this happens because four-wave mixing mixes wavelengths in a photon-number conserving manner, which means that fluctuations (vacuum or otherwise) in the input wavelengths will cause the output intensity at some colours to increase at the expense of others. From this argument, it is clear that any conservative mode-mixing nonlinearity can enable this phenomenon, for example, spatially multimode nonlinear systems such as multimode fibres and waveguides.

To make this idea more concrete, we show experimentally that even combining two wavelengths, the collective noise can be about an order of magnitude lower than the individual wavelength noises, manifesting this noise immunity owing to correlations. In Fig. 5, we consider the example of the sum of photon numbers of two colours (of wavelengths  $\lambda, \lambda'$ ) in the output, denoted  $n_{OUT} = n_{\lambda} + n_{\lambda'}$  (which is realized by using the programmable filter to send two narrow bands of wavelengths to the detector). The noise in  $n_{OUT}$  comes from quantum and other noises in the individual wavelength components of the initial pulse (Fig. 5a), even those wavelengths that have negligible mean intensity. Certain pairs of wavelengths  $\lambda, \lambda'$  at the output show very low sensitivity to noise at wavelengths where the input intensity is concentrated (the input band). This occurs when fluctuations in the input band lead to opposite shifts in the intensities of  $\lambda$  and  $\lambda'$ . For these pairs, the noise is set by vacuum fluctuations in inputs, which are initially dark, at wavelengths close to that of the red-shifted soliton (where  $F_i = 1$  and the derivative is non-zero, compared with the pump wavelengths where the derivative is zero, even though the  $F_i \gg 1$ ). By contrast, other pairs, where fluctuations lead to shifts in the same direction for the two wavelengths, have strong sensitivity to noise in the input band

(Fig. 5b,c). The signature of cancellation is a low noise in the intensity of certain pairs, much lower than the intensity noise of either of the individual wavelengths alone. This effect is consistent with anti-correlated shifts in the two wavelengths in response to noise in many input channels. That noise will not cancel out in the individual wavelength noises, but it will in the 'pair noises'.

The theoretical predictions for the pair noise and the noise relative to the individual wavelengths, resulting from equation (1), are shown in Fig. 5d,e. We measure the pair noises and relative noises by using our programmable filter to send two wavelengths to the detector and measuring intensity fluctuations. We scan all possible pairs of wavelengths. The results are shown in Fig. 5f,g, which clearly corroborate the theory, and indicate that at the level of pairs of wavelengths, certain pairs can be an order of magnitude more resilient to noise than the individual wavelengths.

#### **Discussion**

Our results are very likely to extend to a range of nonlinear systems. In fact, we expect that in a wide variety of multimode nonlinear systems, there are hidden low-noise states with quantum levels of noise, which only become accessible when filtering the light in the right basis. Similar to the case of 'temporally multimode' systems considered here, these low-noise states should emerge almost independently of noise in the input, enabling the development of a new generation of light sources, which operate at the highest powers while also featuring genuinely quantum noise and correlations.

We briefly discuss guidelines for finding these effects in other nonlinear systems. Finding the minimum noise corresponds to finding the filter function, which maximizes the mutual anticorrelation between the transmitted modes. It is worth noting that for filtering like we have done, binary 0-1 filters are best, as anything else (for example, a 0-0.8filter) would introduce vacuum fluctuations and add more noise. Owing to the intricate correlations created by nonlinearity, the filters can be complex (for example, having gaps like in Fig. 3). Further, the exact position and width of the different bins (for example, frequency bins in our case) would matter, if the intensity-intensity correlation function varies rapidly over the wavelength scale of one bin. In many cases, the resulting output is adequate for many applications (for example, if one is using the laser to pump a system with broadband response). While the question of how to realize the cleanest output with the highest power and lowest noise is an exciting direction for future work, we point out one possibility. By coherently shaping the input (for example, controlling the intensity and phase of different inputs), one can tune the output correlations, allowing tunability in the intensity and noise of the output.

Intense quantum light sources should facilitate the generation of quantum states of electrons, phonons and other excitations in strongly driven materials. A number of effects associated with high-power lasers could be explored for this purpose, including topological solitons<sup>26,27</sup>, self-similar systems<sup>28,29</sup> and spatially multimode systems<sup>30–33</sup>. Even more broadly, there is a great range of effects that are being investigated, whose 'quantum optical nature' either has not been touched at all or contains many basic open questions. Examples of such systems and effects include complex parametric oscillators<sup>34–36</sup>, integrated squeezed light sources<sup>37–41</sup>, disordered systems<sup>42,43</sup>, soliton microcombs<sup>44–46</sup>, nonlinear parity-time symmetric systems<sup>47</sup>, topological lasers<sup>48,49</sup>, topological spatial solitons<sup>27,50</sup> and high-harmonic generation<sup>51,52</sup>.

#### Online content

Any methods, additional references, Nature Portfolio reporting summaries, source data, extended data, supplementary information, acknowledgements, peer review information; details of author contributions and competing interests; and statements of data and code availability are available at https://doi.org/10.1038/s41566-025-01677-2.

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# **Data availability**

The data used to generate the plots in Figs. 2, 3 and 5 are available via figshare at https://doi.org/10.6084/m9.figshare.28664672. All data that support the other findings of this study are available from the corresponding author upon reasonable request. Source data are provided with this paper.

# **Code availability**

The scripts used to implement the model used in this study are available from the corresponding author upon reasonable request.

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### **Author contributions**

N.R. developed the theoretical framework and models used to analyse the data, with contributions from S.Z.U. and J.S. N.R. and S.Z.U. analysed the data. S.Z.U. led the construction of the experimental set-up and the data collection with contributions from D.S., Y.S., J.S., S.X. and N.R. The concept of noise immunity was conceived by N.R. and developed in discussions with S.Z.U., I.K. and M.S. The paper was written by N.R. with input from S.Z.U., D.S., J.S., Y.S., S.X., C.R.-C., M.Y.S., I.K. and M.S. All authors contributed to the reading and revision of the paper.

# **Competing interests**

The authors declare no competing interests.

## **Additional information**

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